

Invasive species triggers a massive loss of ecosystem services through a trophic cascade

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Contributed by Stephen R. Carpenter, February 17, 2016 (sent for review January 8, 2016; reviewed by Chris Luecke, David Strayer, and Norman D. Yan)

Despite growing recognition of the importance of ecosystem services and the economic and ecological harm caused by invasive species, linkages between invasions, changes in ecosystem functioning, and in turn, provisioning of ecosystem services remain poorly documented and poorly understood. We evaluate the economic impacts of an invasion that cascaded through a food web to cause substantial declines in water clarity, a valued ecosystem service. The predatory zooplankton, the spiny water flea (*Bythotrephes longimanus*), invaded the Laurentian Great Lakes in the 1980s and has subsequently undergone secondary spread to inland lakes, including Lake Mendota (Wisconsin), in 2009. In Lake Mendota, *Bythotrephes* has reached unparalleled densities compared with in other lakes, decreasing biomass of the grazer *Daphnia pulicaria* and causing a decline in water clarity of nearly 1 m. Time series modeling revealed that the loss in water clarity, valued at US\$140 million (US\$640 per household), could be reversed by a 71% reduction in phosphorus loading. A phosphorus reduction of this magnitude is estimated to cost between US\$86.5 million and US\$163 million (US\$430–US\$810 per household). Estimates of the economic effects of Great Lakes invasive species may increase considerably if cases of secondary invasions into inland lakes, such as Lake Mendota, are included. Furthermore, such extreme cases of economic damages call for increased investment in the prevention and control of invasive species to better maximize the economic benefits of such programs. Our results highlight the need to more fully incorporate ecosystem services into our analysis of invasive species impacts, management, and public policy.

invasive species | ecosystem service | eutrophication | *Bythotrephes* | *Daphnia*

Despite growing recognition of the importance of ecosystem services (1) and the harm caused to ecosystems by invasive species (2, 3), linkages between species invasions and ecosystem services are rarely made (4–6). Investments in the prevention of species invasions may sustain ecosystem services. However, the effects of invasions are rarely quantified in monetary terms that assess damages to services alongside the costs and ecological mechanisms of restoration options (6, 7). Invasive species are a major threat to freshwater ecosystems (8) and thereby, endanger several ecosystem services that are essential for human wellbeing.

Freshwater ecosystems are a cornerstone of human society, providing drinking water, fisheries, pollution dilution, recreation, and other goods and services (9). Valuation of these services is critical for public policy (10, 11), but many of the services provided by freshwater ecosystems are not monetized (12, 13), leaving them overlooked and poorly integrated into decision frameworks (1, 3). Water quality of lakes and reservoirs has been degraded by phosphorus (P) pollution, leading to loss of recreation and aesthetic value, decreased lakeshore property values, beach closures, fish kills, harmful blooms of cyanobacteria, and loss of water clarity (14). *Daphnia*, a genus of freshwater zooplankton, improves water quality by consuming algae (15, 16). Accordingly, lakes are sometimes managed to support large *Daphnia* populations by reducing the abundance of their predators (15, 17).

The spiny water flea, *Bythotrephes longimanus* (hereafter *Bythotrephes*), which is nonnative in North America, is a voracious

zooplanktivore that has the capacity to consume more zooplankton than fish and other invertebrate planktivores combined (18). Despite this planktivory and large documented ecological impacts on zooplankton communities (19, 20), *Bythotrephes* has not been found to have cascading effects on lake primary production and water clarity (21). The lack of cascading effects of *Bythotrephes* invasion is perhaps because the productive lakes most vulnerable to impaired water clarity are thought to be relatively unsuitable for *Bythotrephes* establishment (22).

Bythotrephes was detected in the well-studied eutrophic Lake Mendota in the fall of 2009 at some of the highest densities on record ($>150\text{ m}^{-3}$; mean open water density). The invasion was of immediate concern, because a preferred prey of *Bythotrephes*, *Daphnia pulicaria*, has been the focal point of Lake Mendota's food web management, supporting the lake's fishery (23) and maintaining clear water through grazing algae (24) (Fig. 1). Lake Mendota is located within an agricultural watershed and receives large amounts of P from farm runoff, reducing water quality by stimulating algal growth (25) (Fig. 1). This ecosystem service provided by *D. pulicaria* has delivered huge economic benefits, providing recreational value to citizens who have been estimated to be willing to pay US\$140 million (present-day value) for 1 m of water clarity (1.6- to 2.6-m change in summer clarity) (26, 27).

Results and Discussion

Since the detection of *Bythotrephes* in 2009, average water clarity in Lake Mendota has declined by 0.9 m (Fig. 2F) alongside a 60% reduction in *D. pulicaria* biomass (Fig. 2B). In addition, there was a decrease in total phosphorus (TP) (Fig. 2D), despite no clear change in P loading (Fig. 2E), and an overall increase in

Significance

Invasive species represent a largely unquantified threat to ecosystem services. Although investment in the prevention of species invasions may sustain ecosystem services, these effects of invasions are rarely measured in monetary terms useful to decision makers. We quantify the economic damages of the degradation of an important ecosystem service, water clarity, caused by invasion by the spiny water flea. We find that the costs of restoring this service, US\$86.5 million–US\$163 million, are comparable with the willingness to pay for the service itself: US\$140 million. This finding highlights the severity of invasive species' impacts when their damages to ecosystem services are considered. Costs of invasive species' secondary spread aggregated across many invasive species and ecosystem services may be large.

Author contributions: J.R.W. and M.J.V.Z. designed research; J.R.W. performed research; J.R.W., S.R.C., and M.J.V.Z. analyzed data; and J.R.W., S.R.C., and M.J.V.Z. wrote the paper.

Reviewers: C.L., Utah State University; D.S., Cary Institute of Ecosystem Studies; and N.D.Y., York University.

The authors declare no conflict of interest.

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This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1600366113/-DCSupplemental.

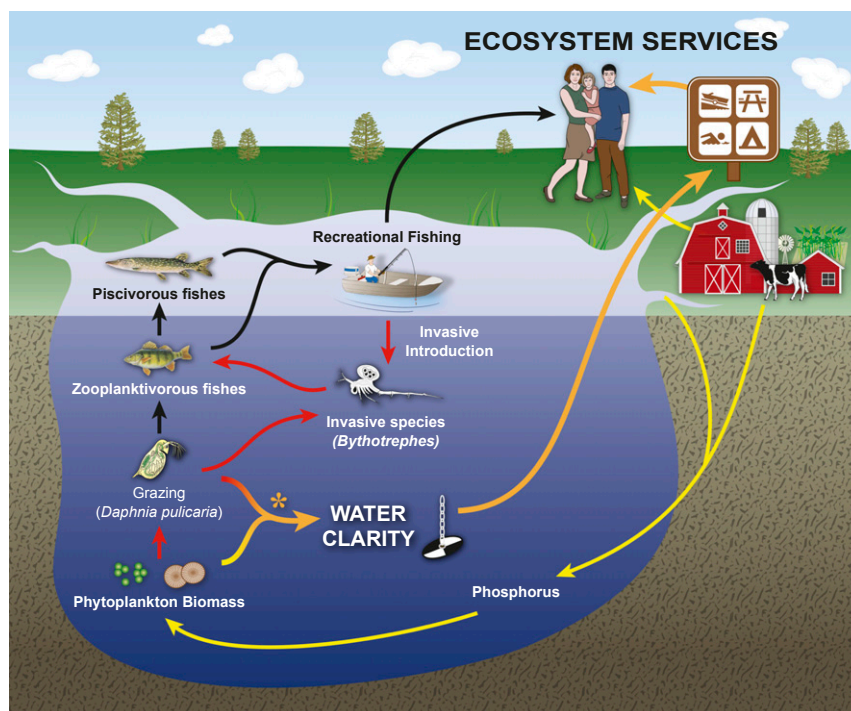


Fig. 1. Arrows represent connections among major components of the socioecological system: Lake Mendota. The introduction of *Bythotrephes* (red arrows) is presented here in the context of existing pathways affecting water clarity (orange arrows), a key ecosystem service in the lake, such as agricultural runoff (yellow arrows), and top-down control of the food web (black arrows). *Increasing phytoplankton biomass resulting from increased nutrient input or decreased grazing decreases water clarity; there are no direct options for the control or eradication of *Bythotrephes*.

total grazing zooplankton biomass (Fig. 2C) (17% overall and 56% increase in non-*D. pulicaria* grazers). These findings show a cascading impact of *Bythotrephes* that has not been previously documented in other lakes (21) and that is unusually large for an invertebrate predator (28). Possibly, this effect is related to the feeding mode of *Bythotrephes* vs. other invertebrate predators (18, 29, 30), and this topic could be addressed by additional research.

The strongest effects of *Bythotrephes* on *D. pulicaria* are observed in the fall (Fig. 2B), when *Bythotrephes* is most abundant (Fig. 2A). These effects occur at a time critical to the overwintering success of *Daphnia*, which may explain declines that

linger into the spring (Fig. 2B). Despite a compensatory increase in other zooplankton grazers (e.g., *Daphnia mendotae*), spring water clarity declined because of an overall decline in algae filtration rates by zooplankton. This decline further reveals the distinct advantage in filtration efficiency of *D. pulicaria* (31). Notably, *Daphnia* of all species collapsed from fall of 2014 to spring of 2015, including the less efficient but more predation-resistant *D. mendotae*. Before 2014, *D. mendotae* increased with the *Bythotrephes* invasion in Lake Mendota (Fig. 2C) as reported in other lakes (32, 33). Although not as efficient of a grazer as *D. pulicaria*, *D. mendotae* does provide better water clarity relative to smaller, more selective grazers, like copepods (24). If *D. mendotae*

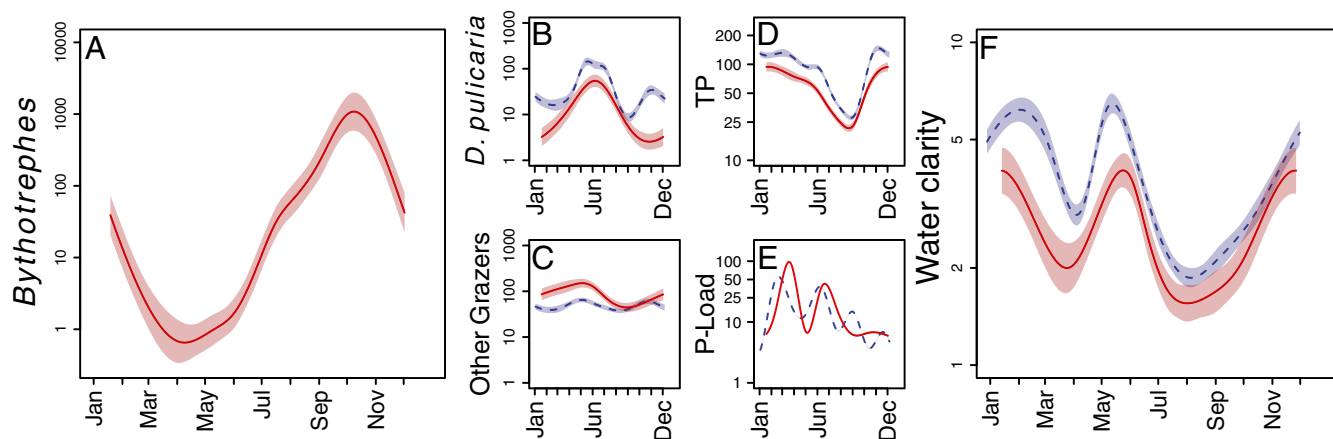


Fig. 2. Seasonal dynamics pre-*Bythotrephes* (blue dashed lines; 1995–2007) and post-*Bythotrephes* (red line; 2009–2014) of (A) *Bythotrephes* (micrograms meter⁻³), (B and C) zooplankton grazers (milligrams meter⁻³), (D and E) P dynamics (micrograms TP liter⁻¹ and kilograms P day⁻¹, respectively), and (F) water clarity (Secchi depth in meters) are plotted as a smoothed generalized additive model function of day of the year. Shaded areas represent 1 SE. Note that all y axes are log scaled.

measurements of ecosystem consequences in terms useful to managers (41). We have shown how an invasive species altered a lake food web, amplifying the harmful effects of cultural eutrophication and impairing water clarity, thereby reducing the benefits that humans derive from lakes. Water quality targets for the lake are more difficult and expensive to achieve as a result of the invasion. These economic damages followed a trophic cascade triggered by a voracious predator that originated in Eurasia and invaded through the Great Lakes and overland to Lake Mendota. Ecological mechanisms as well as economic ones must be analyzed together to bring ecosystem services into decision processes regarding species invasion (12).

Methods Summary

Lake Mendota. Lake Mendota is a 39.6-km² dimictic (mixes in spring and fall) and culturally eutrophic lake located adjacent to Madison, Wisconsin (25). Maximum and mean depths are 25.3 and 12.7 m, respectively, and the lake has a mean water residence time of roughly 4 y. A large portion of the land use within total drainage area in the watershed (602 km²) is agricultural and urban. Lake Mendota is the largest, deepest, and most upstream lake in the Madison Chain of Lakes connected by the Yahara River. Therefore, P dynamics in Lake Mendota have important implications for waters downstream, like the southern chain lakes—Lake Monona, Lake Waubesa, and Lake Kegonsa—as well as the Rock River, which flows into the Mississippi River.

Time Series. We obtained time series data of Lake Mendota's water clarity (Secchi depth), zooplankton community (species abundance and mean length), TP concentrations in the surface waters, and surface temperature from the North Temperate Lakes Long-Term Ecological Research program database (<https://lter.limnology.wisc.edu/>). Samples are taken on a monthly basis in the early spring and late fall, at least once during ice cover (all variables are sampled or observed through the ice), and fortnightly during the open season (roughly May to October). Data are available from 1995 to 2014 (2013 in the case of TP in Fig. 2D). Zooplankton abundance was converted to biomass using mean lengths and length to dry weight equations (42). Daily P loading measurements are available through the US Geological Survey ([usgs.gov](https://www.usgs.gov/)). Rather than calculate the TP load into the lake directly, we use the Yahara River at the Windsor Site as a proxy for loading into the lake (total load = 4.5 × Yahara River at Windsor load; $R^2 = 0.97$). We summed daily P loading over fortnightly time steps. Clarity, zooplankton biomass, and P loading were log-transformed, and all variables were converted to fortnightly means and then, z scored. To visualize seasonal dynamics of pre- and post-*Bythotrephes* invasion time series, we fit cyclic cubic regression splines of day of the year to the log-transformed data for time periods both before (1995–2007) and after (2010–2014) the year of *Bythotrephes* detection (2009) using generalized additive models with the package mgcv in R (43). We exclude 2008 and 2009 as transition years. All statistical analyses were conducted in R (44).

Statistical Analysis: MARSS–Model Fitting. We used a MARSS to analyze the dynamics of water clarity in Lake Mendota using the MARSS package in R (45). The model takes the following form:

$$\begin{bmatrix} x_s \\ x_c \end{bmatrix}_t = \begin{bmatrix} B_s & C \\ 0 & B_c \end{bmatrix} \begin{bmatrix} x_s \\ x_c \end{bmatrix}_{t-1} + w_t, w \sim MVN\left(0, \begin{bmatrix} Q_s & 0 \\ 0 & Q_v \end{bmatrix}\right) \\ \begin{bmatrix} y_s \\ y_c \end{bmatrix}_t = \begin{bmatrix} x_s \\ x_c \end{bmatrix}_t + v_t, v \sim MVN\left(0, \begin{bmatrix} R_s & 0 \\ 0 & R_v \end{bmatrix}\right).$$

Observations (shown in the lower equation) comprise interacting system variables, such as Secchi depth, *D. pulicaria* biomass, and biomass of other (non-*D. pulicaria*) grazers, in vector y_s and covariates, such as P loading and surface temperature, in vector y_c (observations from 1995 to 2014). All observations are transformed to z scores. The observation vector estimates a partitioned vector of true values of system variable x_s and covariate x_c , with error v having covariances given by R_s and R_v , respectively. System dynamics

(shown in the upper equation) involve a square transition matrix, with partitions for system interactions B_s , covariate effects on system variables C , and covariate changes over time B_c . System error w has covariances given by Q_s and Q_v corresponding to system variates and covariates, respectively. MARSS models are fit with maximum likelihood using a combination of the Kalman filter and an expectation maximization algorithm.

Model fits estimated all elements of B_s and Q_s (interactions among system variables and their variances and covariances) and diagonal elements of B_c and Q_v (autoregressive coefficients of covariates and their variances). We allowed the model to estimate terms along the R matrix diagonal (observation variances). The final model structure was selected using Akaike Information Criterion and previously published ecological interactions among variables. Here, we allow interactions between zooplankton grazers and known drivers of water clarity, like P loading, zooplankton, and surface temperature (i.e., arrows in Fig. 3). Temperature was allowed to affect all variates. Model selection (Table S1) and residual analysis (Figs. S1 and S2) can be found in [Additional MARSS Modeling Information](#).

Estimating Economic Costs. To estimate the effect of P loading on water clarity, we made predictions using our MARSS model under varying grazing (pre- and post-*Bythotrephes*; i.e., high and low grazing from *D. pulicaria*) and P loading (–99% to +100%) scenarios under post-2009 surface temperature conditions and long-term average P loading conditions. We chose to investigate improving water clarity through P loading reduction as opposed to other methods (e.g., chemical treatment or biological control) because of existing efforts to reduce P loading into Lake Mendota (26, 27) and additional benefits to water quality of lakes downstream of Lake Mendota (25).

The costs of P load reductions are estimated using a report by Strand Associates, Inc. from 2013 (35) (pdf available). The goal of the *Yahara CLEAN Engineering Report* was to develop a list of action items that would result in a 50% P load reduction into Lake Mendota in addition to the costs of those items. The report takes into account not only the efficiency of each action item (in US dollars per 1 lb P reduced) but also, nonmonetary factors that will influence the prioritization of action items, like implementability, social acceptance, benefits visible to the public, water management, maintaining functional farmland and farming culture, nutrient distribution, reliability of the action item or technology, and ancillary benefits. P loading reduction costs are estimated as present-day value over a 20-y project period. The *Yahara CLEAN Engineering Report* also details the necessary investment for a maximum implementation plan or 86% reduction (97% reduction of direct drainage sources) in P loading. The cost of a 50% reduction was estimated to be US\$70 million over a 20-y period, and the cost of an 86% reduction was estimated to be US\$177 million over a 20-y period. We estimated the economic costs of offsetting *Bythotrephes* impact using table 4.01–2 in ref. 35, which details the costs, efficiency, and P load reduction of each action item. We bound the estimate by summing the most and least cost-efficient (in US dollars per 1 lb P reduced) items that would achieve the 71% P load reduction.

Updating Willingness to Pay Estimates from the Work by Stumborg et al. (26).

Stumborg et al. (26) estimate Madison's willingness to pay for 1 m of water clarity in Lake Mendota at US\$353.53 per household. We adjust this number to present value or buying power, US\$645.49, using the Consumer Price Index Inflation Calculator (www.bls.gov/data/). We also updated the number of households in Dane County from the 1990 census of 155,200 households to the 2014 estimate by the US Census Bureau of 217,100 households ([census.gov](https://www.census.gov/)).

ACKNOWLEDGMENTS. We thank Kirsten Rhude, Ted Bier, Elizabeth Runde, and Emily Stanley for North Temperate Lakes Long Term Ecological Research program data collection; Bill Provencher and Dan Phaneuf for economic advice; Naomi Walsh and Carol Dizack (University of Wisconsin Media Solutions) for assistance with graphics and editing; and Tony Ives, Randy Jackson, Alex Latzka, Alison Mikulyuk, and Scott Van Egeren for comments. This work was funded by the Wisconsin Department of Natural Resources, NSF North Temperate Long-Term Ecological Research Program Grants DEB-0217533 and DEB-1440297, and NSF Water Sustainability and Climate Program Grant DEB-1038759.

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